

MODEL COMPACT PENTRU TRANZISTOARE MOS SUBMICRONICE PENTRU APLICATII ANALOGICE

Gheorghe Brezeanu, Andrei Sevcenco



*Facultatea de Electronica, Telecomunicatii și
Tehnologia Informației
Universitatea POLITEHNICA Bucuresti*



Cuprins

- ❖ *Evolutia tehnologiei CMOS*
- ❖ *Saturatia vitezei. Degradarea mobilitatii*
- ❖ *Model compact al tranzistorului MOS*
- ❖ *Comparatii model –date experimentale*
- ❖ *Concluzii*

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Microelectronica

- ❖ Tranzistorul bipolar – începutul microelectronicii
- ❖ Descoperire importanta a sec. 20
- ❖ Dec. 1947 patent-tranz.cu contact punctiform-amplificator
- ❖ Sept. 1951, tranzistorul cu joncțiuni

The Revolution Begins

Invented 60 years ago, the transistor is a key building block of today's digital world. Perhaps the most important invention of the 20th century, transistors are found in many devices and are the building blocks of computer chips. Intel, the largest manufacturer of computer chips, continues to innovate to help PCs and laptops become smaller, faster, sleeker and more energy-efficient. Many new applications and inventions powered by transistors have impacted all of our lives over the past 60 years.



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Circuite Integrate- aplicații

Impactul industriei semiconductoare este uriaș în multiple domenii:

- PC/ laptopuri
- Carduri
- Comunicații / telefonie mobilă
- Multimedia(tv, jurnale electronice)
- Sisteme audio & video portabile
- Electronică medicală
- Electronică auto
- GPS – Global Positioning System
- Aplicații militare
- Explorarea spațiului

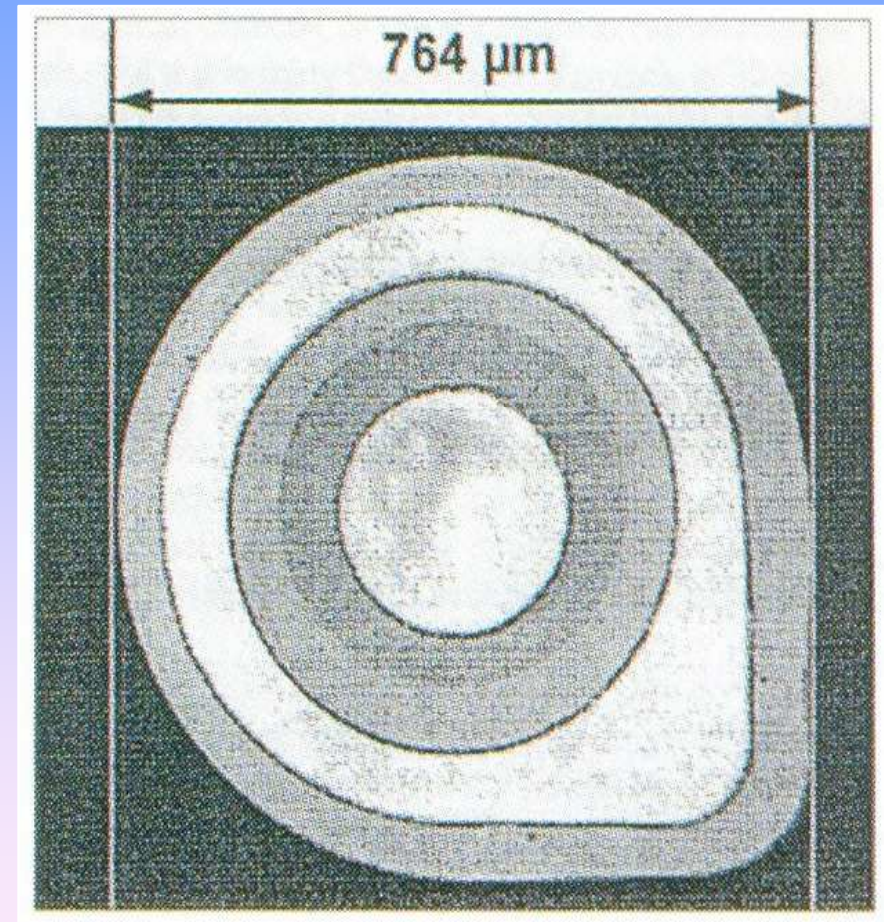


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Inceputul CI

- ⊕ 1959- primul TB planar
 - Diametru -30 inch
 - Dimensiunea minimă-3 inch
- ⊕ 1962 – primul CI
 - Produs de Fairchild
 - 4 tranzistoare + 6 rezistoare
 - 6 fire de conexiune
 - Încapsulat în TO5
- ⊕ 1965- Micrologic circuit
 - Produs de Fairchild
 - 50 componente

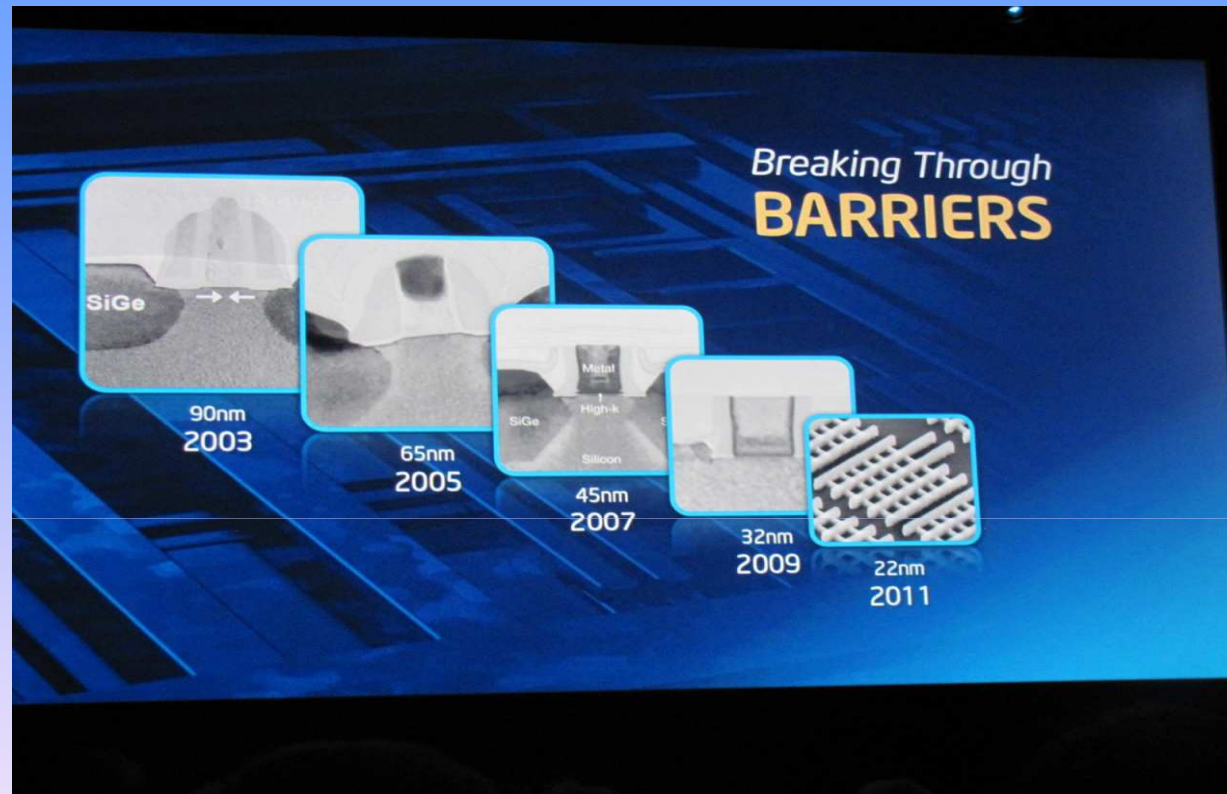


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Scalarea lungimii canalului

Dimensiuni nanometrice



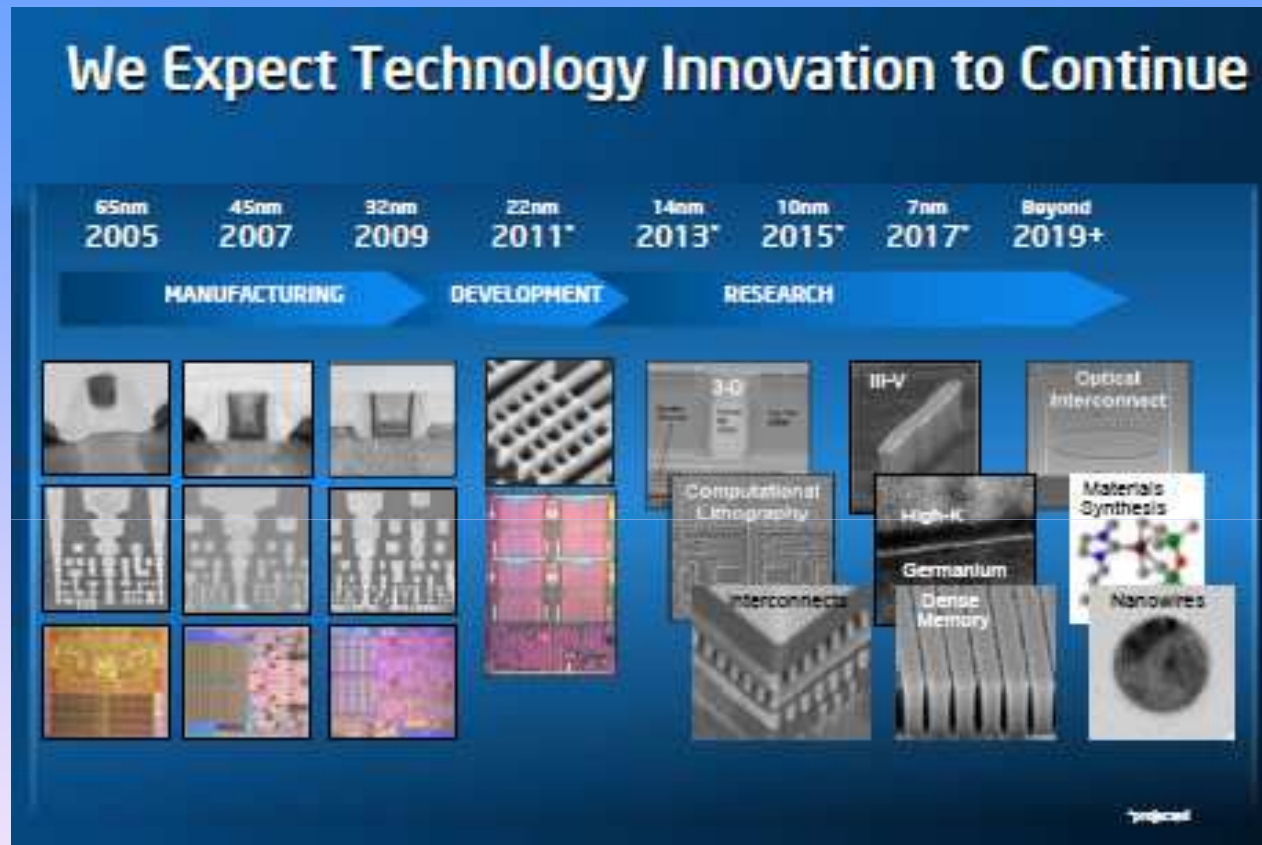
- ❖ Tehnologii CMOS
- ❖ 2 ani rata de innoire
- ❖ Circuite VLSI digitale

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Scalarea lungimii canalului

Previziuni



- ❖ Nanofire
- ❖ Conexiuni optice
- ❖ Litografie computationala

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INTEL - Evolutia microprocesoarelor Multi-cores



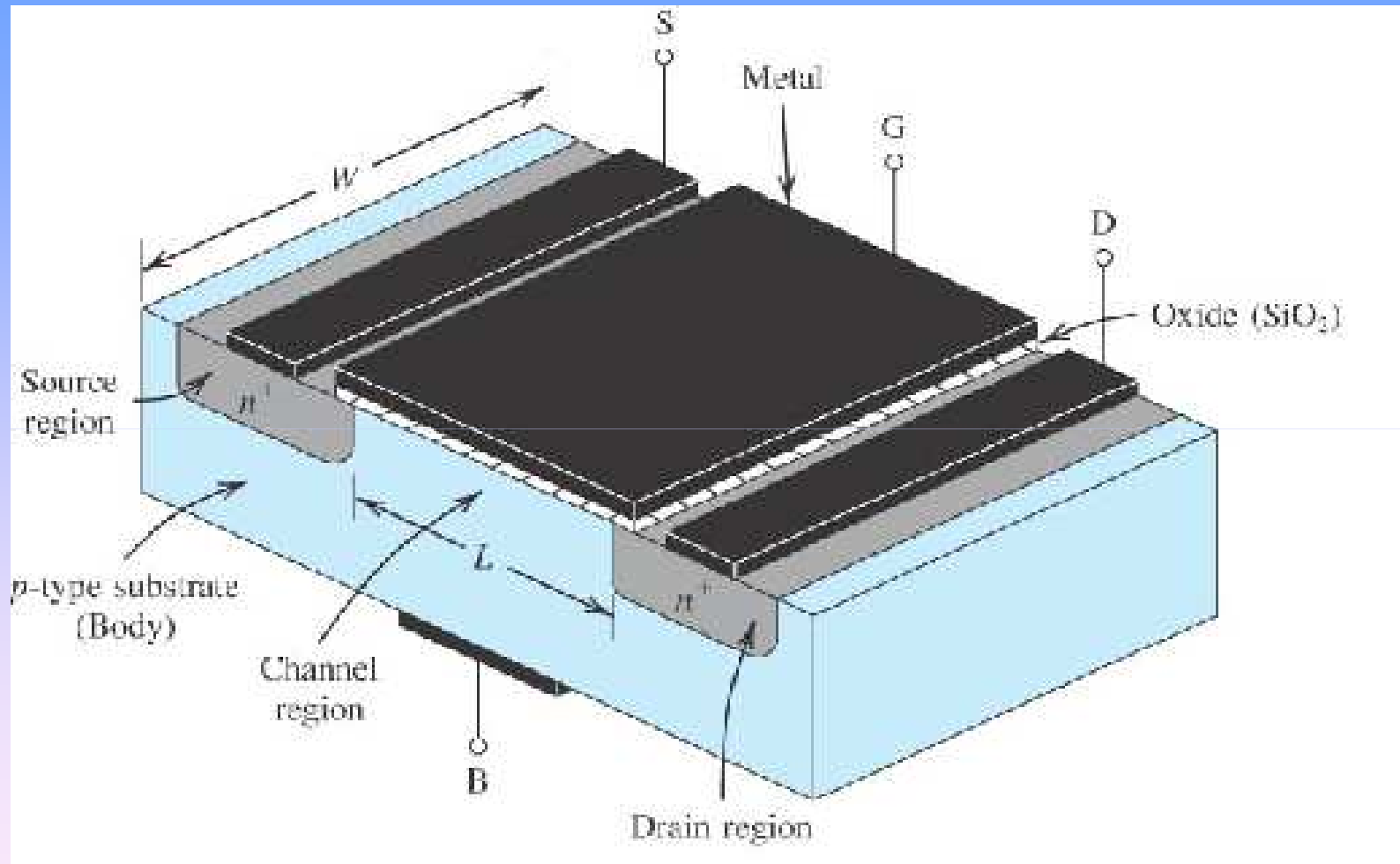
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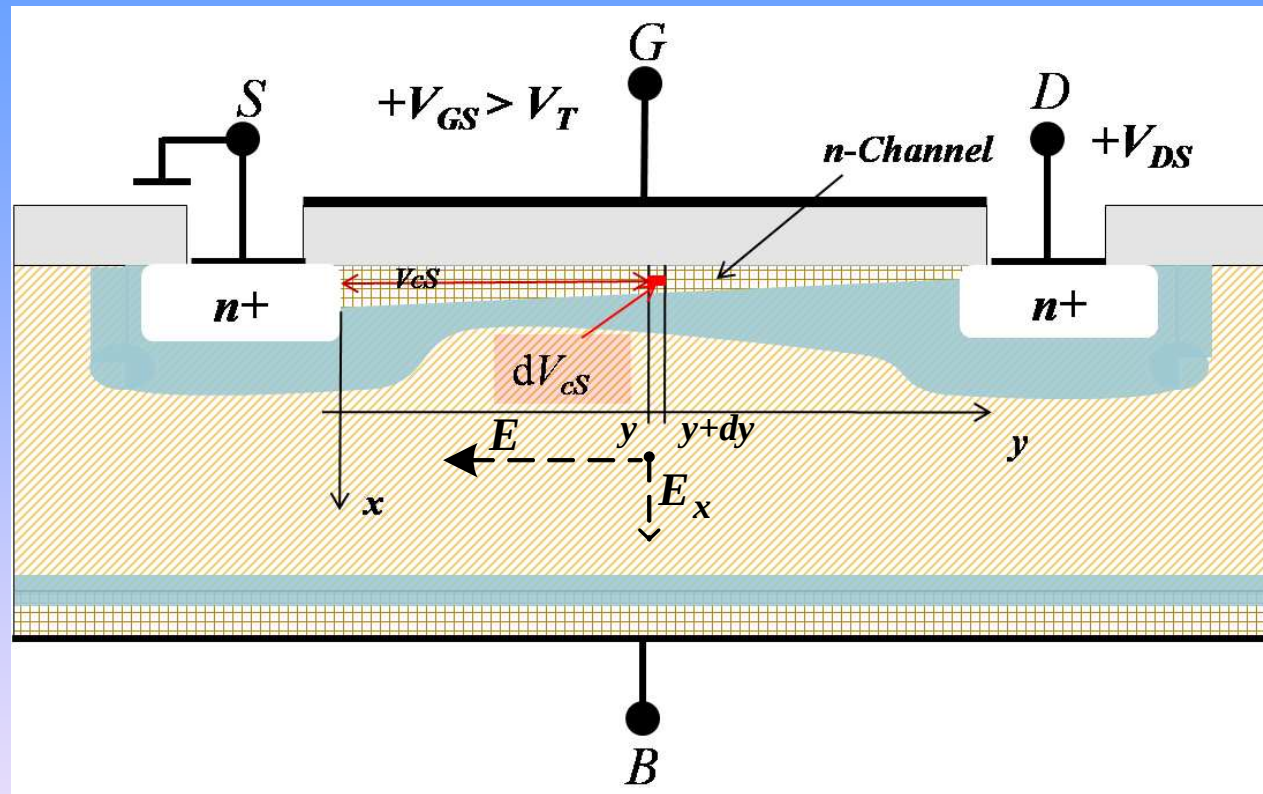
Microelectronics

- ⊕ Prețul unui tranzistor din CI echivalează azi costul tipăririi unui caracter (literă) într-o publicație oarecare;
- ⊕ Acum o memorie DRAM de *4MB* si *4milioane* de tranzistoare costă mai puțin decât un tranzistor în 1960;
- ⊕ Nr. de caractere din toate tipăriturile depășește cu doar un ordin de mărime nr. de tranzistoare incluse în CI fabricate până în prezent.

nMOS - Structura tridimensională



nMOS -Efecte de canal scurt



- ❖ ξ_x - campul transversal - degradarea mobilitatii
- ❖ ξ - campul longitudinal – saturatia vitezei



Degradarea mobilitatii

$$\mu(y) = \frac{\mu_0}{1 + \frac{\xi_x(y)}{\xi_{x,c}}}$$

- ❖ $\xi_x(y) \cong \frac{V_{OV} + 2V_T - V_{cs}(y)}{6t_{ox}}$ - campul electric transversal
- ❖ $\xi_{x,c} = 1.5V/\mu m$ - campul transversal critic
- ❖ $V_{OV} = V_{GS} - V_T$ - tensiunea de comandă efectivă
- ❖ V_T - tensiunea de prag
- ❖ t_{ox} - grosimea oxidului de poartă



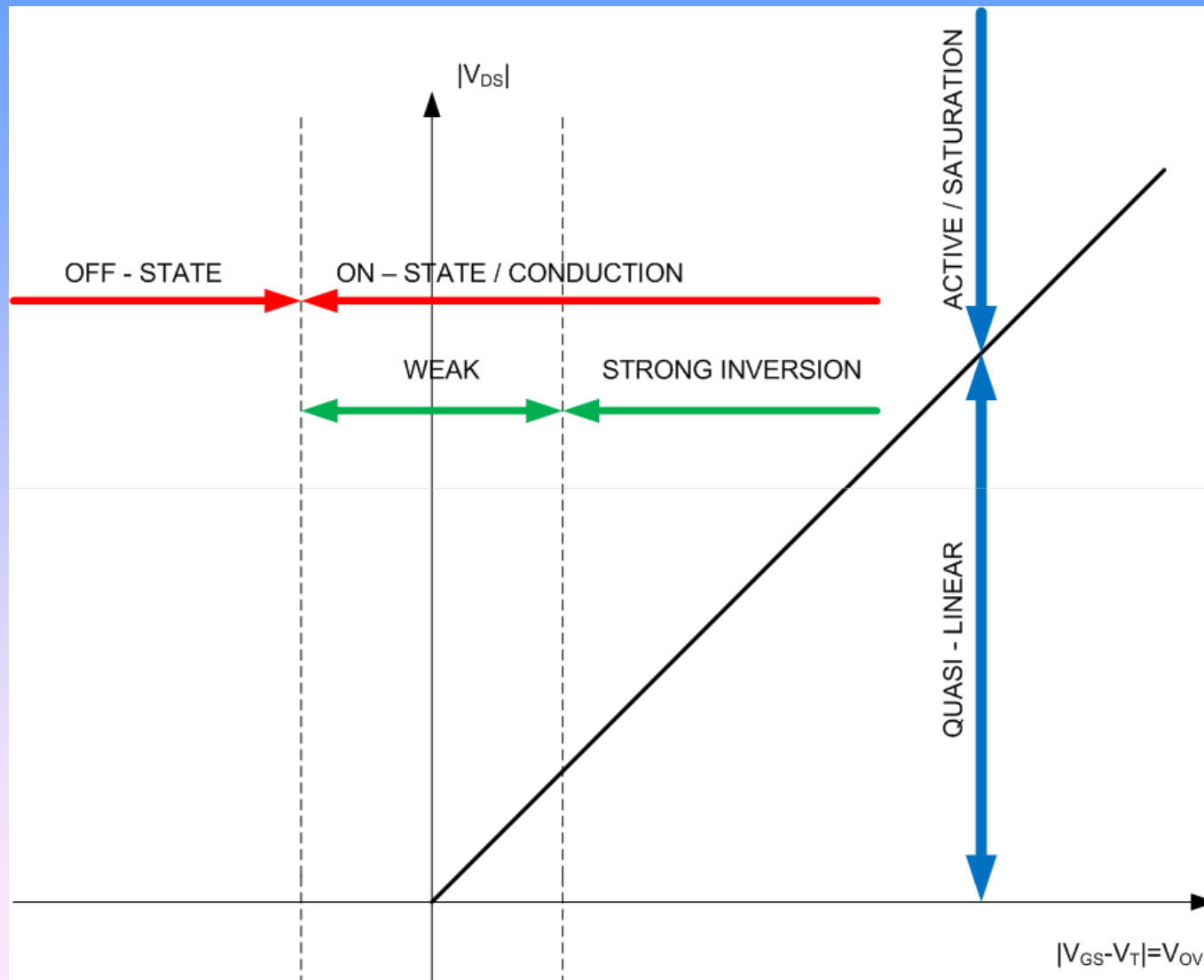
Saturatia vitezei

$$v(y) = \frac{\mu \xi(y)}{\left(1 + (\xi(y)/\xi_c)^\alpha\right)^{1/\alpha}}$$

- ❖ $v(y)$
 - viteza purtatorilor mobili în canal
- ❖ $\xi(y) = \frac{V_{cs}}{L}$
 - campul electric vertical/longitudinal
- ❖ $\xi_c = 1.5V/\mu m$
 - campul (vertical) critic
- ❖ $\alpha = 1/\alpha = 2$
 - pt. goluri(*p*- MOS)/electroni(*n* -MOS)



MOS – regiuni de funcționare



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Modelarea in inversie puternica(1)

$$I_D = Wv(y)|Q_I(y)|$$

$$Q_I(y) = C_{ox} (V_{GS} - V_T - V_{cs}(y))$$

- Sarcina purtatorilor mobili din canal
- Capacitatea oxidului de poarta

$$I_D = W[C_{ox} (V_{GS} - V_T - V_{cs}(y))] \frac{\mu(y) \frac{dV_{cs}}{dy}}{\left[1 + \left(\frac{dV_{cs}}{dy} / \xi_c\right)^\alpha\right]^{1/\alpha}}$$

$$\int_0^L I_D \left[1 + \left(\frac{dV_{cs}}{dy} / \xi_c\right)^\alpha\right]^{1/\alpha} dy = WC_{ox}\mu_0 \int_0^{V_{DS}} \frac{V_{OV} - V_{cs}(y)}{1 + \frac{V_{OV} + 2V_T - V_{cs}(y)}{V_{GS,C}}} dV_{cs}$$

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Modelarea in inversie puternica (2)

$$I_D = \frac{W}{L} \cdot \mu_0 C_{ox} \cdot \frac{1}{1 + \frac{V_{DS}}{V_{DS,C}}} \left[V_{GS,C} \cdot V_{DS} + V_{GS,C} \cdot (V_{GS,C} + 2V_T) \cdot \ln \left(1 - \frac{V_{DS}}{V_{OV} + 2V_T + V_{GS,C}} \right) \right]$$

$V_{DS,C} = aL\xi_c$ - Tensiunea de drenă critică

$V_{GS,C} = 6\xi_{x,c}t_{ox}$ - Tensiunea de poarta critică

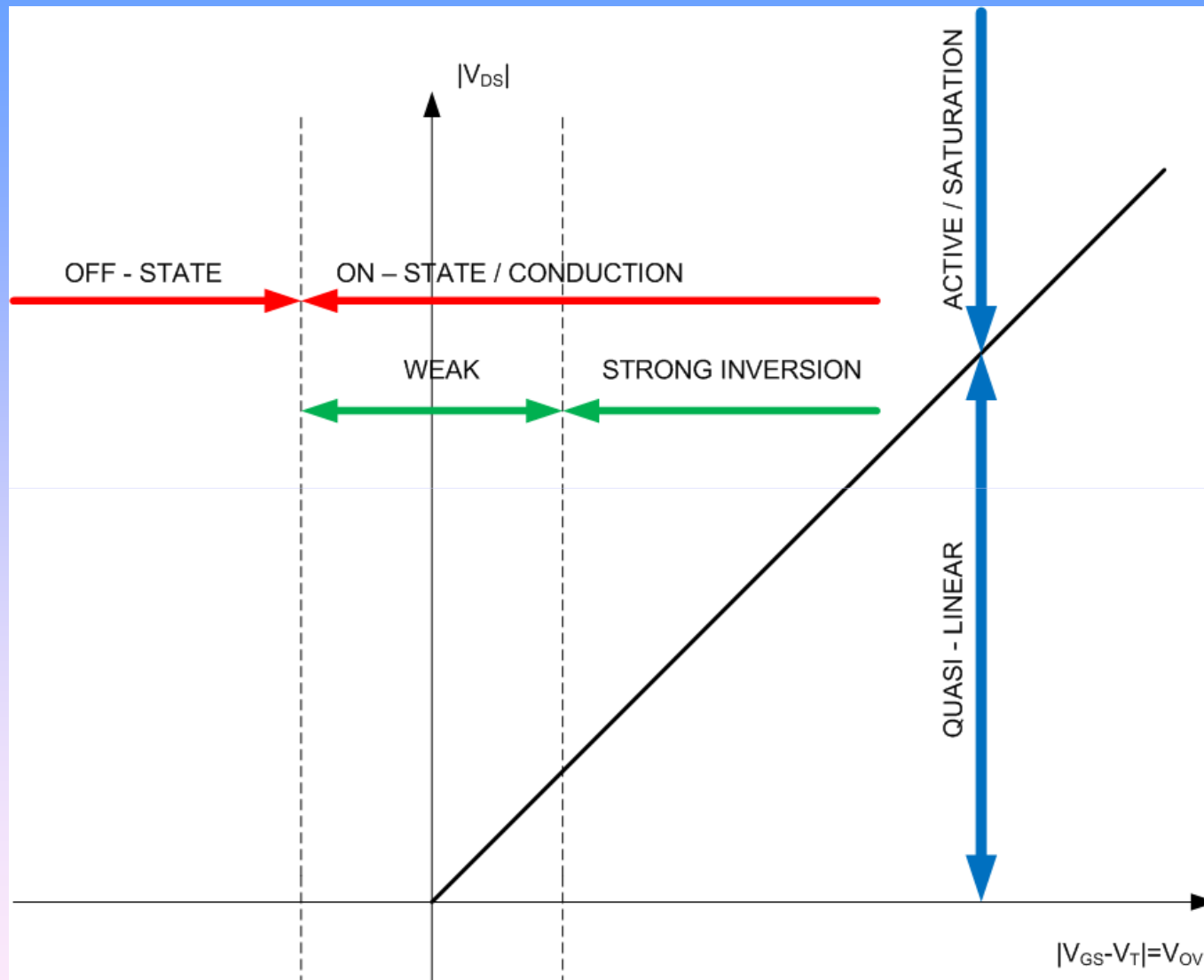
$$\ln(1+x) \cong x - \frac{x^2}{2} \quad pt. \quad x \ll 1$$

$$I_D \cong \frac{W}{L} \cdot \mu_0 C_{ox} \frac{1}{1 + \frac{V_{OV} + 2V_T}{V_{GS,C}}} \cdot \frac{1}{1 + \frac{V_{DS}}{V_{DS,C}}} \left[V_{OV} \cdot V_{DS} - \frac{1}{2} \frac{V_{DS}^2}{1 + \frac{V_{OV}}{2V_T + V_{GS,C}}} \right]$$

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MOS – regiuni de funcționare



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Curentul de drena in zona de trioda

❖ Modelul nou

$$I_D \cong \frac{W}{L} \cdot \mu_{eff} C_{ox} \cdot \frac{1}{1 + \frac{V_{DS}}{V_{DS,C}}} \left[V_{OV} \cdot \left(1 + \overline{V_{OV}} \right) \cdot V_{DS} - \frac{1}{2} \cdot V_{DS}^2 \right]$$

$$\mu_{eff} = \frac{\mu_0}{1 + \frac{2V_T}{V_{GS,C}}} \cdot \frac{1}{\left(1 + \overline{V_{OV}} \right)^2} \quad \text{- Mobilitatea efectivă la campuri longitudinale mici}$$

$$\overline{V_{OV}} = \frac{V_{OV}}{2V_T + V_{GS,C}} \quad \text{- Tensiunea de comanda efectiva normata}$$

❖ Modelul clasic

$$V_{OV} = V_{GS} - V_T \ll V_{GS,C} \quad \text{- Efectul campului transversal-neglijabil}$$

$$V_{DS} \ll V_{DS,C} \quad \text{- Efectul campului longitudinal-neglijabil}$$

$$I_D \cong \frac{W}{L} \cdot \mu_0 C_{ox} \left[V_{OV} \cdot V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

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Curentul de drena in zona activa (1)

❖ Modelul nou

$$I_D = \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_{eff} C_{ox} \cdot V_{DS,act}^2 = I_{D,C} \frac{V_{DS,act}^2}{V_{DS,C}^2}$$

$$V_{DS,act} = V_{DS,C} \left(\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})} - 1 \right) \quad \text{- tensiunea de drena la limita intre zona de trioda si zona activa}$$

$$I_{D,C} = \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_{eff} C_{ox} \cdot V_{DS,C}^2 \quad \text{- curentul de drena critic}$$

❖ Modelul clasic $(V_{OV} = V_{GS} - V_T \ll V_{GS,C} \quad V_{DS} \ll V_{DS,C})$

$$V_{DS,act} = V_{DS,sat} = V_{OV} = V_{GS} - V_T$$

$$I_D \cong \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_0 C_{ox} \cdot V_{DS,act}^2 = \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_0 C_{ox} \cdot V_{DS,OV}^2$$

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Curentul de drena in zona activa (2)

Cazuri limită

$$I_D = \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_{\text{eff}} C_{\text{ox}} \cdot V_{\text{DS,act}}^2 = I_{D,C} \frac{V_{\text{DS,act}}^2}{V_{\text{DS,C}}^2}$$

❖ *Tensiune de comandă mică* ($V_{\text{OV}} \ll V_{\text{GS,C}}$ $V_{\text{OV}} \ll V_{\text{DS,C}}$)

$$V_{\text{DS,act}} \cong V_{\text{OV}} \quad I_D = \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_0 C_{\text{ox}} \cdot V_{\text{OV}}^2$$

❖ *Tensiune de comandă medie*

$$V_{\text{DS,act}} = V_{\text{DS,C}} \quad I_D = I_{D,C} = \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_{\text{eff}} C_{\text{ox}} \cdot V_{\text{DS,C}}^2$$

❖ *Tensiune de comandă mare* $V_{\text{OV}} \gg V_{\text{DS,C}}$

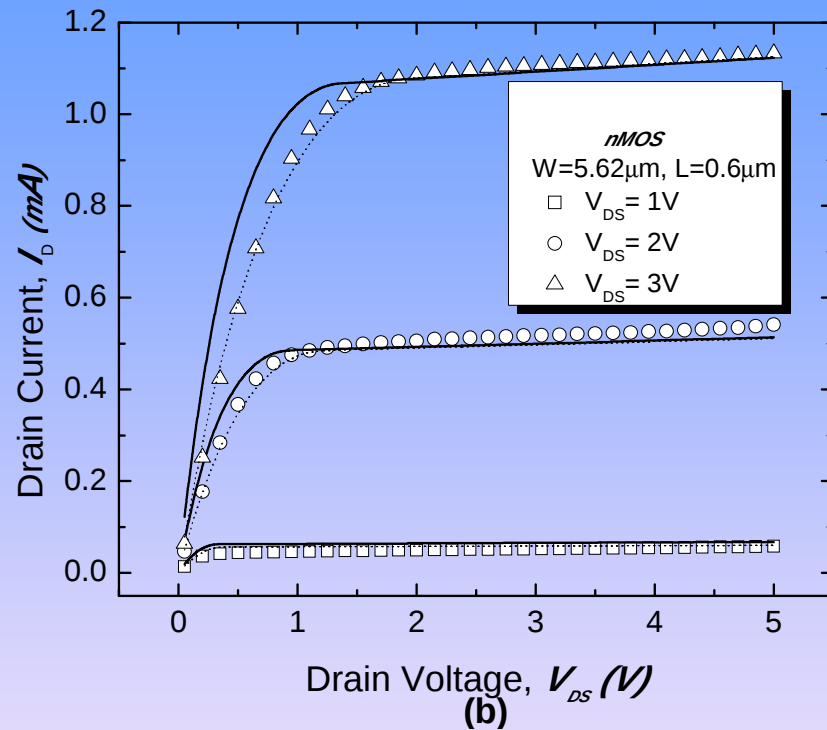
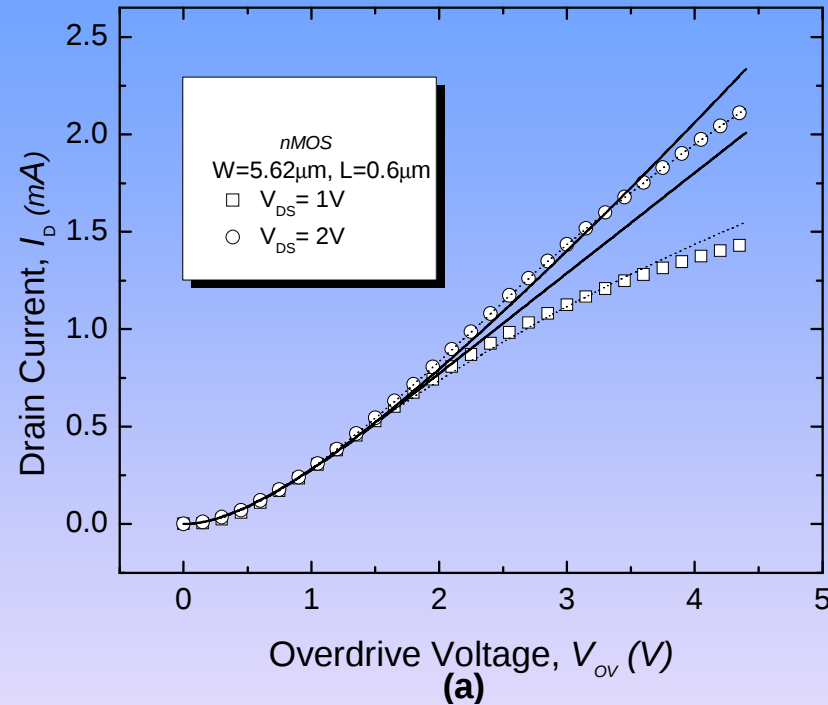
$$V_{\text{DS,act}} \cong \sqrt{2V_{\text{OV}} V_{\text{DS,C}} (1 + \overline{V_{\text{OV}}})}$$

$$I_D \cong \frac{1}{2} \cdot \frac{W}{L} \cdot \mu_0 C_{\text{ox}} \cdot V_{\text{GS,C}} \cdot V_{\text{DS,C}} = \text{const.}$$

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nMOS - comparatie model - experiment



Caracteristici de transfer

Caracteristici de iesire

Date experimentale - simboluri

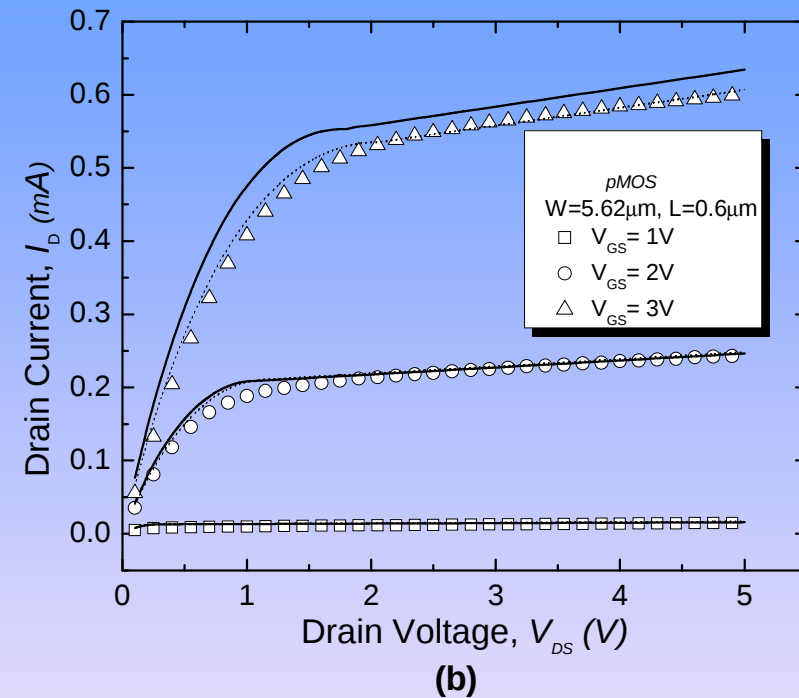
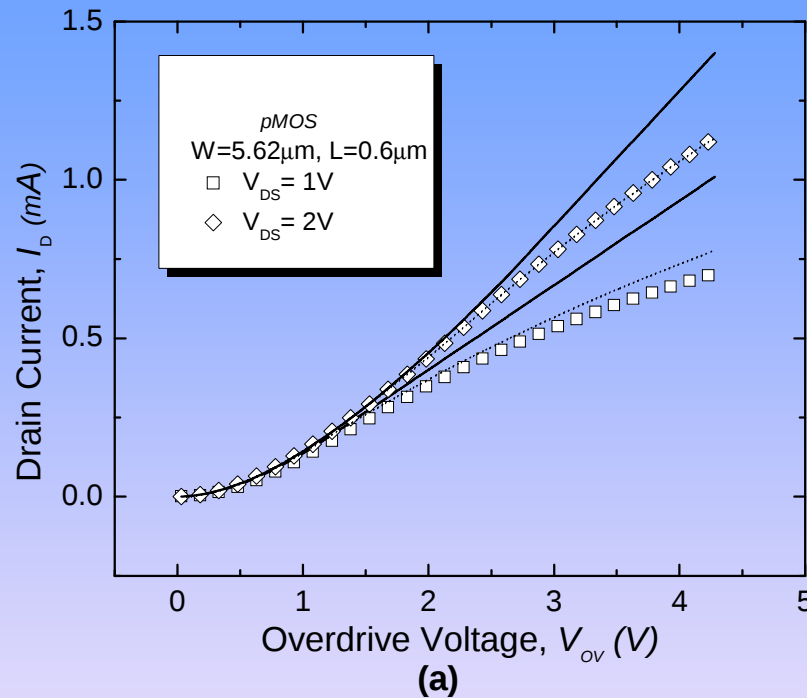
Model complet - linie intrerupta

Model simplu(fara degradarea mobilitatii) - linie continua

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pMOS - comparatie model - experiment



Caracteristici de transfer

Caracteristici de iesire

Date experimentale - simboluri

Model complet - linie intrerupta

Model simplu(fara degradarea mobilitatii) - linie continua

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Comparatie model – experiment

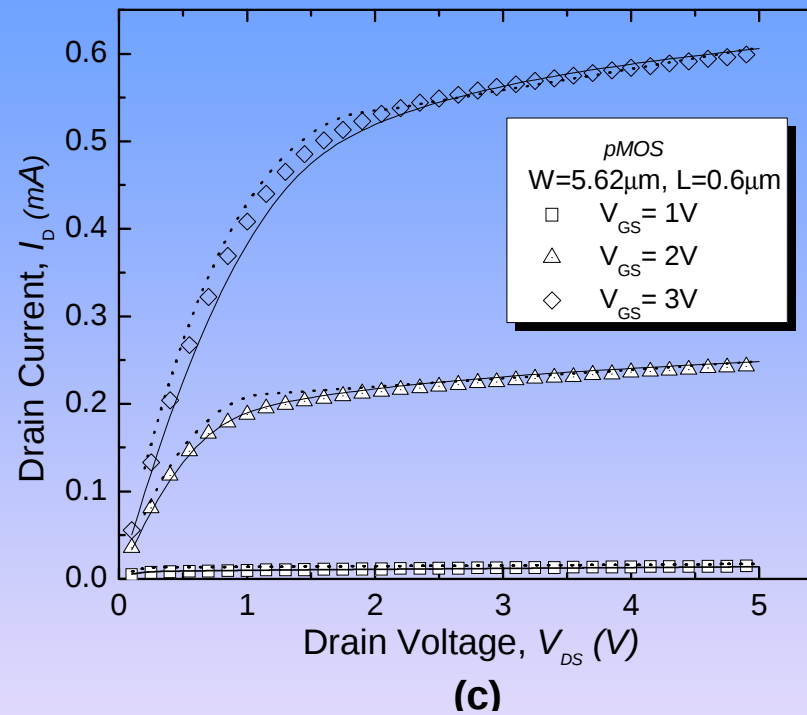
Characteristic	Device	W/L	Model error (%)	
			Simplu	Complet
ID – VDS VGS = 3V	nMOS	0.7/0.6	5.68	0.35
	nMOS	5.62/0.6	4.95	0.08
	pMOS	5.62/0.6	8.22	2.35
ID – VGS VDS = 2V	nMOS	0.7/0.6	2.37	0.36
	nMOS	5.62/0.6	1.7	1.7
	pMOS	5.62/0.6	5.01	0.72

- ❖ Se observa micșorarea erorii pentru modelul complet
- ❖ Motivul este combinarea efectelor de canal scurt

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Comparatie model - experiment - BSIM



Date experimentale - simboluri

Model complet - linie intrerupta

BSIM - linie continua

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Transconductanta - panta tranzistorului

$$g_m = \frac{i_d}{v_{gs}} = \left. \frac{\partial i_D}{\partial v_{GS}} \right|_{I_D, V_{DS}}$$

Parametru dinamic-defineste performantele de amplificare
❖ dependenta de curent

$$g_m = g_{m,c} \frac{1}{1 + \sqrt{I_{D,C}/I_D}} \left(1 + \sqrt{\frac{I_D}{I_{D,C}}} \frac{V_{DS,C}}{2V_T + V_{GS,C}} \right)$$

$$g_{m,c} = \frac{W}{L} \cdot \mu_{eff} C_{ox} \cdot V_{DS,C}$$

❖ dependenta de tensiunea de comanda efectiva

$$g_m = g_{m,c} \left(1 - \frac{1}{\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})}} \right) \left(1 + \frac{2\overline{V_{OV}}}{\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})} + 1} \right)$$

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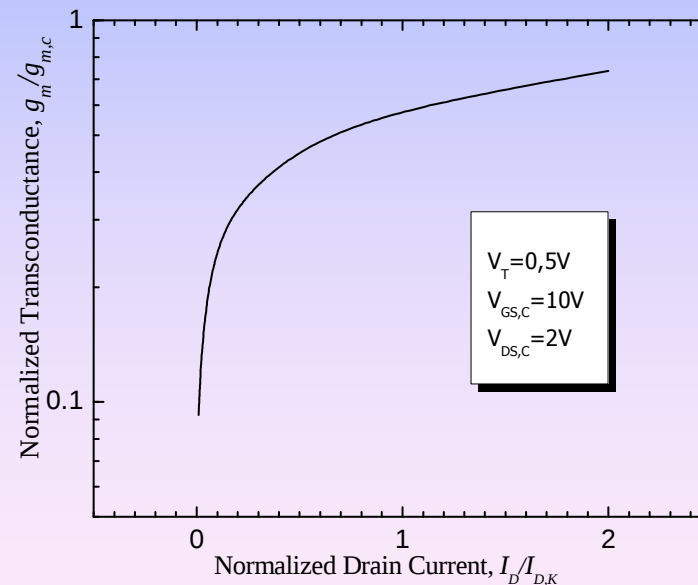
Transconductanta - cazuri limita

- ❖ Curenti mici - saturatia vitezei neglijabilă $I_D \ll I_{D,C}$

$$g_m \cong g_{m,c} \sqrt{\frac{I_D}{I_{D,C}}} = \sqrt{2 \frac{W}{L} \mu_{eff} C_{ox} I_D}$$

- ❖ Curenti mari $I_D \gg I_{D,C}$

$$g_m \rightarrow g_{m,c} = \frac{W}{L} \cdot \mu_{eff} C_{ox} \cdot V_{DS,C} = W \cdot \mu_{eff} C_{ox} \cdot \xi_C$$

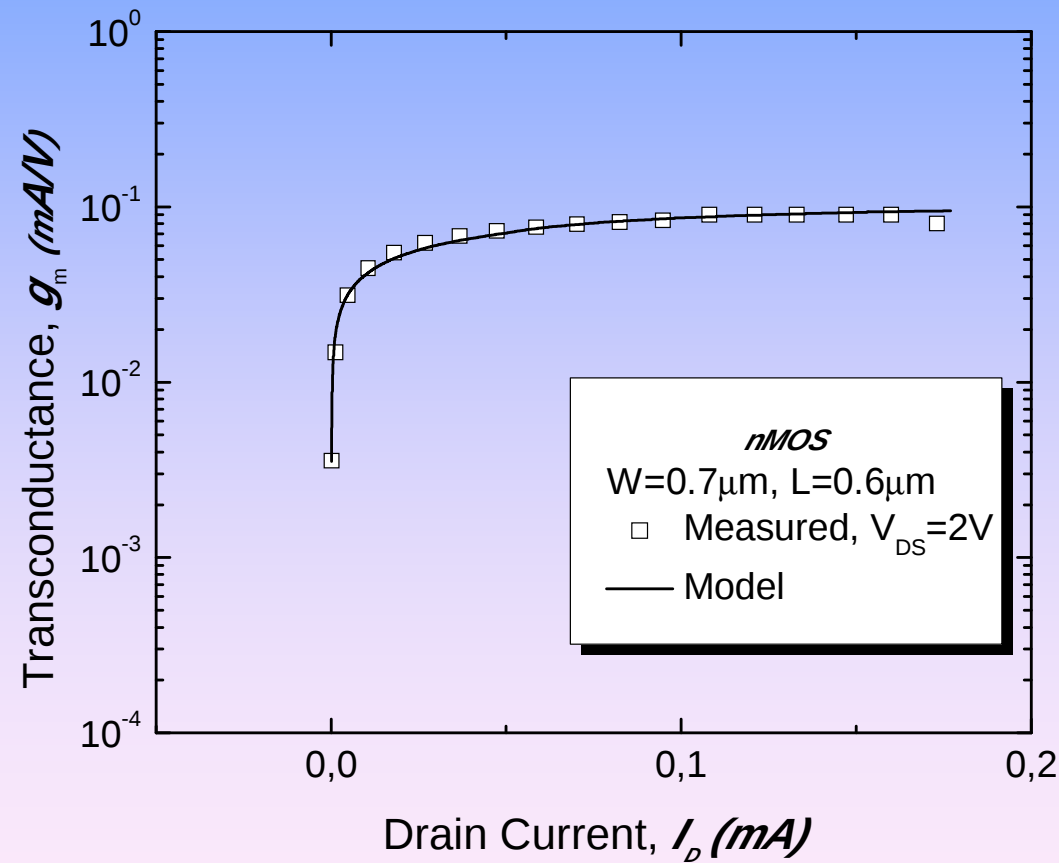


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Transconductanța- dependentă de curent

$$g_m = g_{m,c} \frac{1}{1 + \sqrt{I_{D,C}/I_D}} \left(1 + \sqrt{\frac{I_D}{I_{D,C}}} \frac{V_{DS,C}}{2V_T + V_{GS,C}} \right)$$

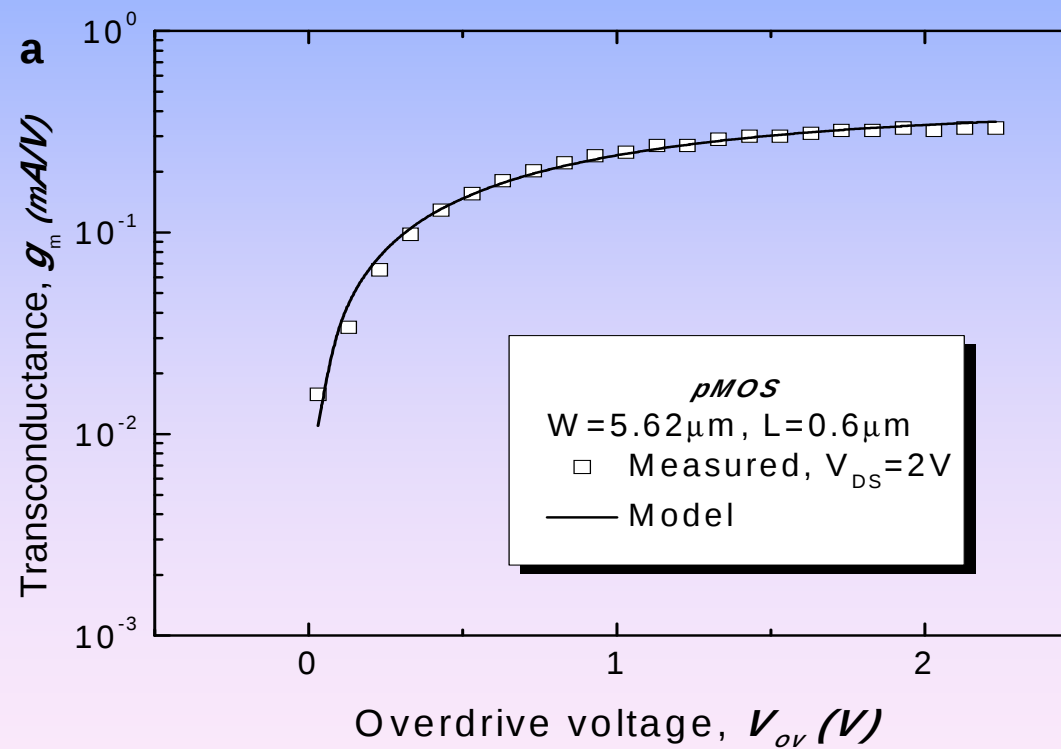


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pMOS-Transconductanța- dependentă de V_{OV}

$$g_m = g_{m,c} \left(1 - \frac{1}{\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})}} \right) \left(1 + \frac{2 \overline{V_{OV}}}{\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})} + 1} \right)$$

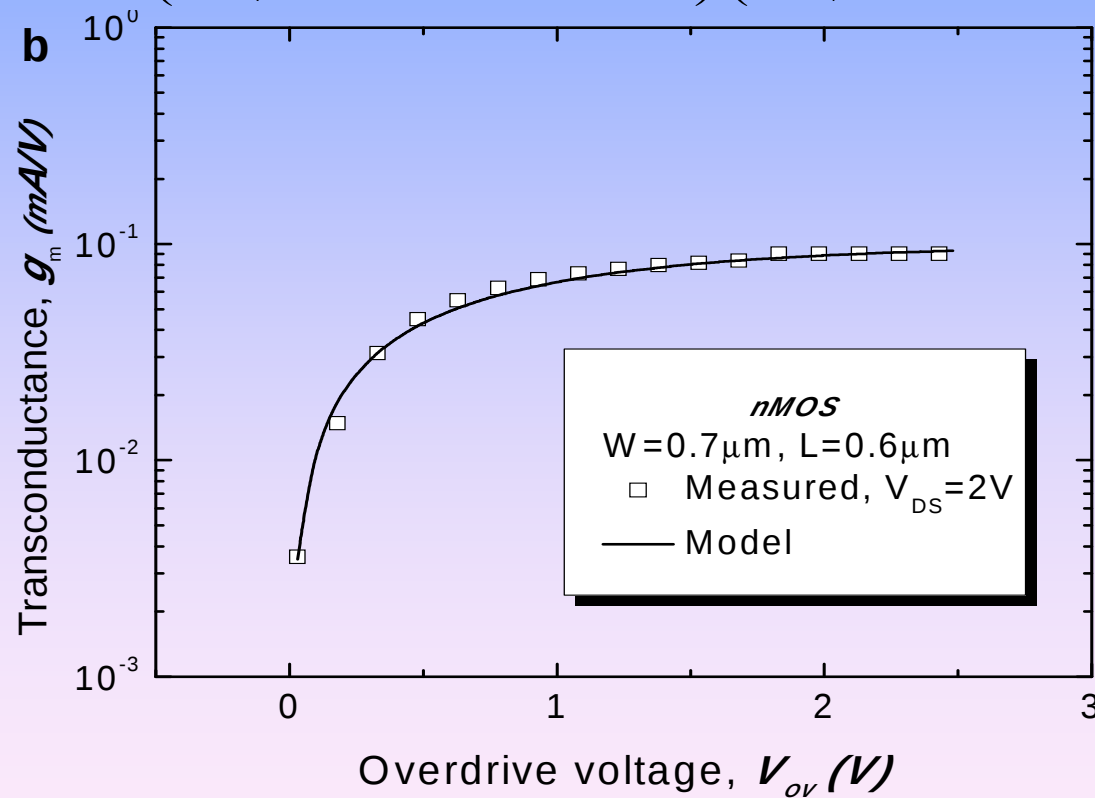


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nMOS-Transconductanța- dependentă de V_{OV}

$$g_m = g_{m,c} \left(1 - \frac{1}{\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})}} \right) \left(1 + \frac{2 \overline{V_{OV}}}{\sqrt{1 + 2 \frac{V_{OV}}{V_{DS,C}} \cdot (1 + \overline{V_{OV}})} + 1} \right)$$



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Concluzii

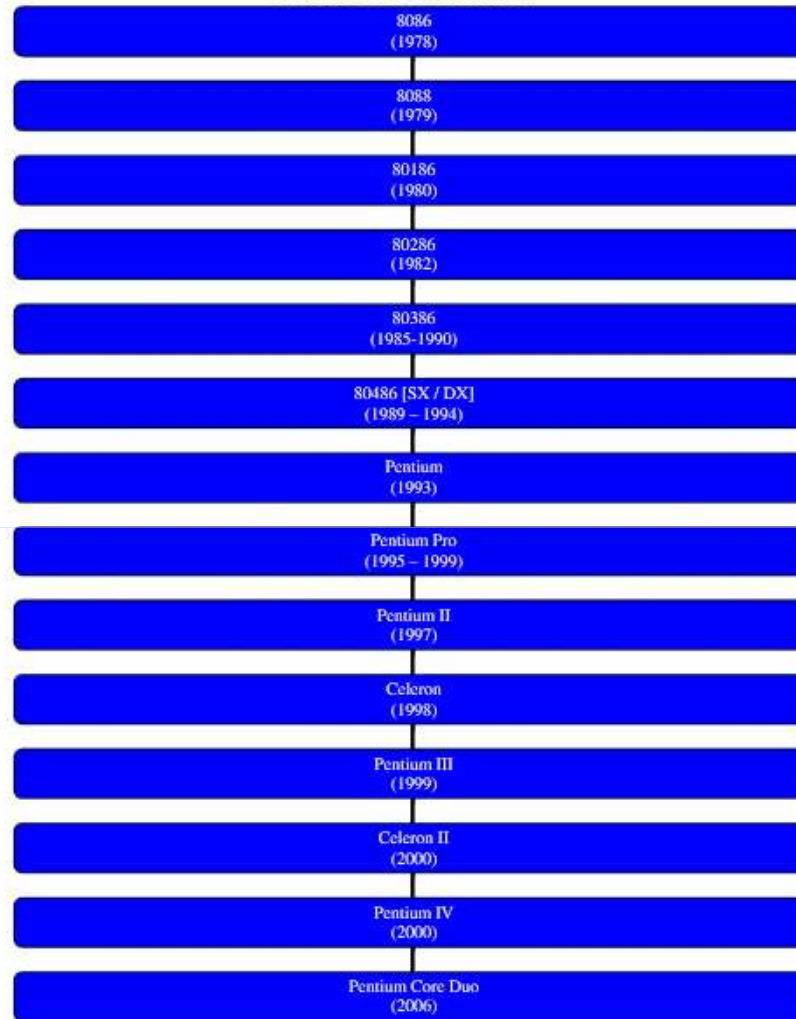
- ⊕ Tehnologiile CMOS evolueaza spre dimensiuni nano
- ⊕ Campul electric in canal devine semnificativ
- ⊕ Campul transvesal $\Rightarrow$ degradarea mobilitatii
- ⊕ Campul longitudinal $\Rightarrow$ saturația vitezei
- ⊕ Model compact – model analitic ce include pentru prima oara efectul combinat al degradarii mobilitatii si saturatiei vitezei
- ⊕ Ecuatii pentru I_D si g_m similare cu cele ale modelului clasic
- ⊕ Modelul este validat prin comparatii cu date experimentale masurate pe n MOS si p MOS fabricate in tehn.CMOS de 0,22um
- ⊕ Rezultate apropiate de BSIM3-model folosit in simulatoare
- ⊕ Poate fi usor implementat in simulatoare
- ⊕ Articol acceptat - **International Journal of Electronics**

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INTEL - Evolutia microprocesoarelor

Intel Processors



1971 - primul microprocesor

1978 - 8086

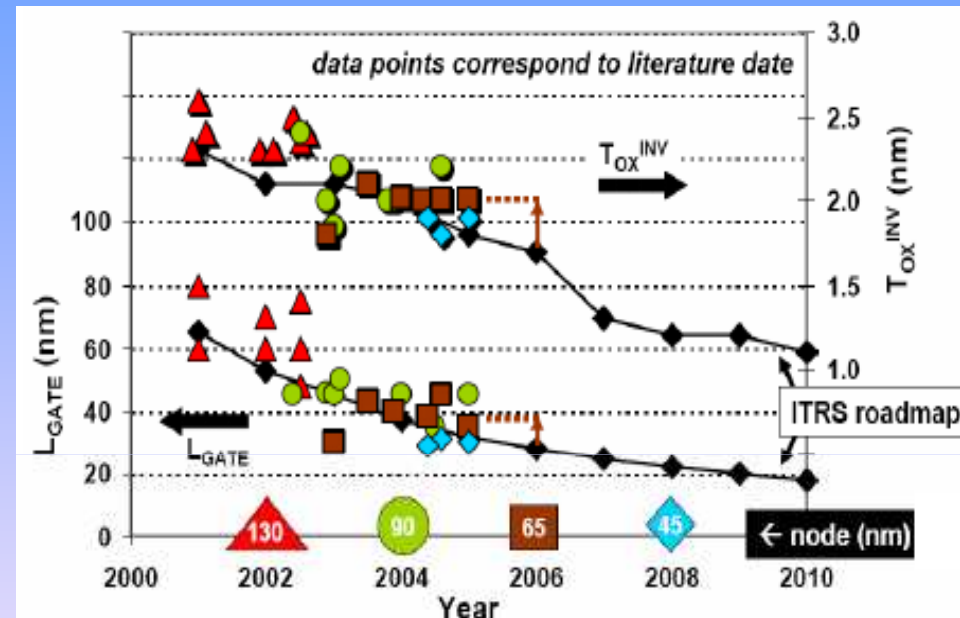
1993 – Pentium

2006 – Pentium dual core

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Scalarea lungimii canalului si grosimii oxidului de poarta



SiO_2 - T_{ox} a scazut pana 1,2 nm (5 distante atomice):

- ❖ curenti de poarta foarte mari,
- ❖ neuniformitate accentuata pe o placheta de 12 inch
- ❖ randamentul si fiabilitatea scad dramatic
- ❖ Dielectrics high k

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